

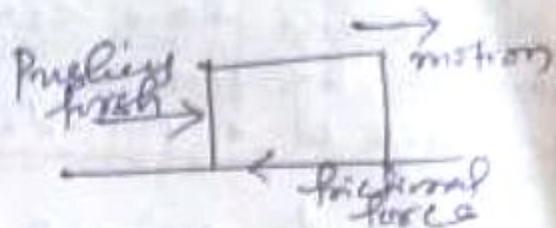
**A LECTURE NOTE  
ON  
TH.1 THEORY OF MACHINE  
SEMESTER -4**



**Prepared by – Mr Sourav Ranjan Pradhan  
Sr. Lecture Mechanical Engineering  
Mechanical Engineering**

**GOVT. POLYTECHNIC,  
MALKANGIRI**

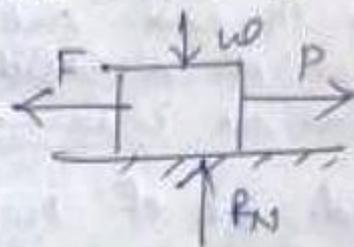
Friction - It is the <sup>limiting</sup> opposing force, which act in the opposite direction of the movement of the upper body, is called "frictional force" or "friction".



Co-efficient of friction :-

The ratio of limiting friction to the normal reaction is known as co-efficient of friction ( $\mu$ ).

$$\mu = F/R_N$$



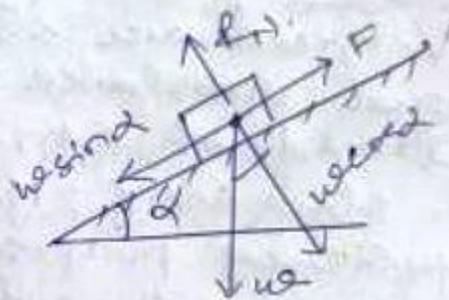
Angle of repose ( $\alpha$ )

$$W \sin \alpha = F$$

$$W \cos \alpha = R_N$$

$$\frac{F}{R_N} = \mu = \frac{W \sin \alpha}{W \cos \alpha}$$

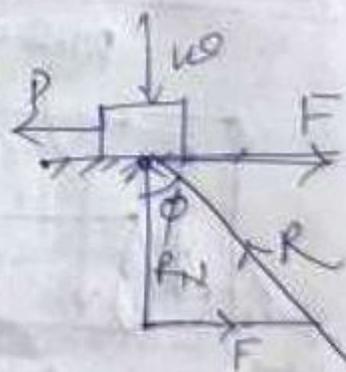
$$\boxed{\mu = \tan \alpha}$$



Angle of friction ( $\phi$ )

It is the angle between resultant of frictional force and normal reaction and the normal reaction.

$$\boxed{\tan \phi = \frac{F}{R_N} = \mu}$$



## Screw friction:-

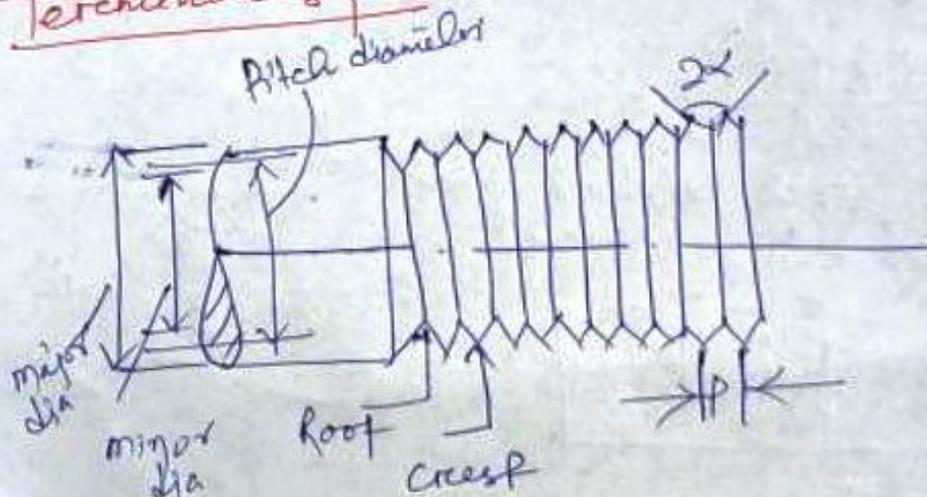
### Friction between nut & Bolt

fasteners have screw thread which are made by cutting a continuous helical groove on a cylindrical surface.

- \* If threads are cut on a outer surface of a solid rod, these are known as external thread.
- \* If the threads are cut on the internal surface of a ~~solid~~ hollow rod, these are known as internal thread.
- \* Threads are of two types  $\left\{ \begin{array}{l} \text{V-thread} \\ \text{square thread} \end{array} \right.$

V-threads are stronger and offer more frictional resistance to motion than square threads. Adv of v thread that it's preventing from slackening. Hence v threads are used for tightening purpose i.e. nut & bolts, where square threads are used in  screw jack, vice screw etc.

## Terminology



**Helix**:- It is the curve traced by a particle mobile moving along a screw thread.

**Pitch**:- It is the distance from a point of a screw to a corresponding point on the next thread, measured parallel to the axis of the screw.

**Lead**:- It is the distance, a screw thread advances axially in one turn.

**Depth of thread**:- It is the distance between top and bottom surface of a thread.

It  $\text{Lead} = \text{Pitch}$  (single threaded screw)

$\text{Lead} = n \times \text{Pitch}$  (multi threaded screw)

**Helix angle**:- It is the slope/inclination of the thread with the horizontal.

$$\tan \alpha = \frac{\text{Lead of screw}}{\text{Circumference of screw}}$$

$$= \frac{P}{\pi d} \text{ (single)}$$

$$= \frac{nP}{\pi d} \text{ (multi)}$$

$\alpha$  = helix angle,

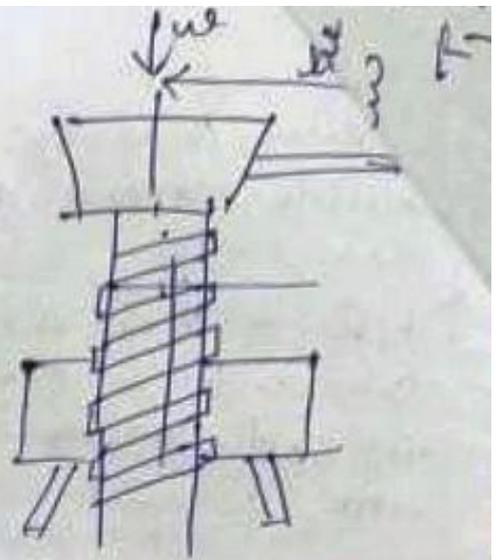
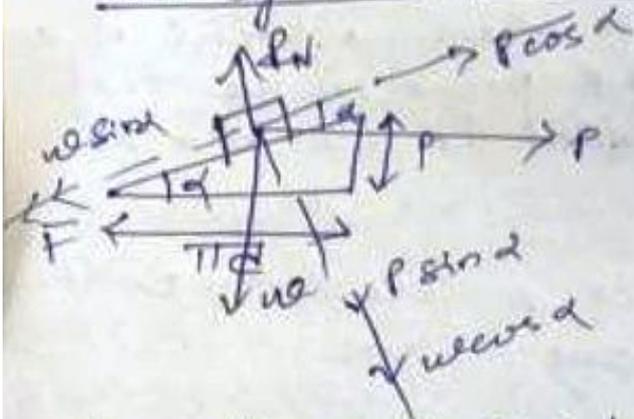
$P$  = pitch

$d$  = mean dia

$n$  = no. of threads in one lead.

## Screw Jack

Torque required to lift the load by screw jack.



$$f_{fr} = P \sin \alpha + \mu W \cos \alpha$$

$$F + \mu W \sin \alpha = P \cos \alpha$$

$$\mu W \cos \alpha + W \sin \alpha = P \cos \alpha$$

$$\mu (P \sin \alpha + \mu W \cos \alpha) + W \sin \alpha = P \cos \alpha$$

$$\mu P \sin \alpha + \mu^2 W \cos \alpha + W \sin \alpha = P \cos \alpha$$

$$W (\sin \alpha + \mu \cos \alpha) = P (\cos \alpha - \mu \sin \alpha)$$

$$W (\sin \alpha + \tan \phi \cos \alpha) = P (\cos \alpha - \tan \phi \sin \alpha)$$

$$W \left( \sin \alpha + \frac{\sin \phi \cdot \cos \alpha}{\cos \phi} \right) = P \left( \cos \alpha - \frac{\sin \phi \cdot \sin \alpha}{\cos \phi} \right)$$

$$W \left( \frac{\sin \alpha \cdot \cos \phi + \sin \phi \cdot \cos \alpha}{\cos \phi} \right) = P \left( \frac{\cos \alpha \cdot \cos \phi - \sin \phi \cdot \sin \alpha}{\cos \phi} \right)$$

$$W (\sin(\alpha + \phi)) = P (\cos(\alpha + \phi))$$

$$P = W \cdot \frac{\sin(\alpha + \phi)}{\cos(\alpha + \phi)}$$

$$P = W \cdot \tan(\alpha + \phi)$$

Force required to overcome friction between the  
screw & nut:

$$T_1 = P \times \frac{d}{2} = \mu \tan(\alpha + \phi) \cdot \frac{d}{2} \quad \text{--- (1)}$$